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School



W I N C H E S T E R

Winchester Entrance and Election

Mathematics I

Monday 26th April 2021, 1400-1530

Time allowed: 1 hour 30 minutes (+5 minutes) You have an additional 5 minutes to give you time to draw out diagrams, which may help with some of the questions.

Total marks: 100

CALCULATORS ARE NOT ALLOWED.

Write your answers on A4 paper, <u>starting each question on a new page</u>. You may use a pencil for diagrams. You should show all your working so that credit may be given for partially correct answers.

Do not be discouraged if you do not finish. If you get more than 60 marks, you will have done well.

Please start Q1 on a new sheet of paper and write your name at the top.

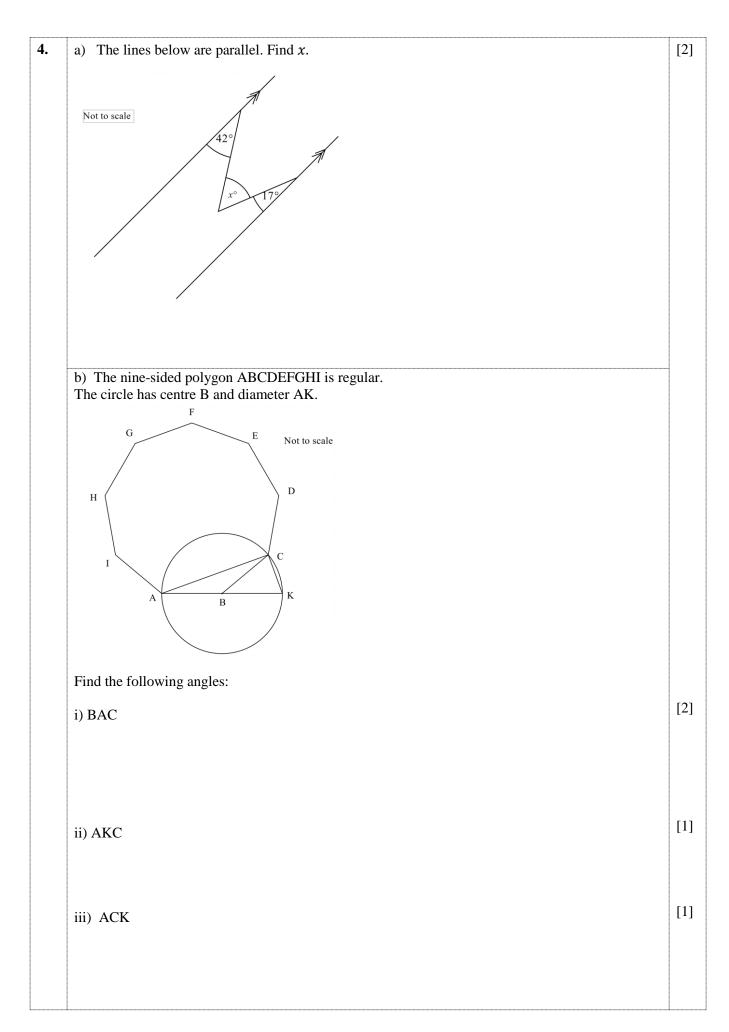
1.	Complete: a) $15^2 =$	b) $2 \times 2 \times 2 \times 2 \times 5 \times 5 \times 5 =$	[1] [1]
	c) 422 – 500 + 579 =	d) $\frac{2+48}{2+3} =$	[1]
	e) $\sqrt{196} \times \sqrt{196} =$	f) $\sqrt{13^2 - 5^2} =$	[1]
	g) 98÷0.014=	h) 99 + 49 × 99 =	[1] [1]

Please start Q2 on a new sheet of paper and write your name at the top.

2.	a) Find $\frac{1}{8}$ of £1024.	b) Find 76% of £25.	[1]
	c) Find 0.7 of £117.	d) Evaluate $\frac{3}{4}$ of $\frac{4}{5}$ of $\frac{5}{6}$ of £556.	[1]
	e) The price of a jumper was £49. It was reduced by 20% then increased by 25% and finally reduced by 30%. What is the new price of the jumper?	f) Evaluate 185×0.32+1.5×3.2.	[2]

3. Find in its simplest form:
a)
$$87 \times \frac{87 + 87}{87}$$
b) $\frac{2}{77} + \frac{1}{143}$
[1]
c) $51 + 4\frac{1}{4}$
d) $\left(\frac{(-18)^3}{(-9)^2} + \frac{(-14)^3}{7^2} + 1\right) \div \frac{(-6)^2}{(-12)^2}$
[2]
[3]

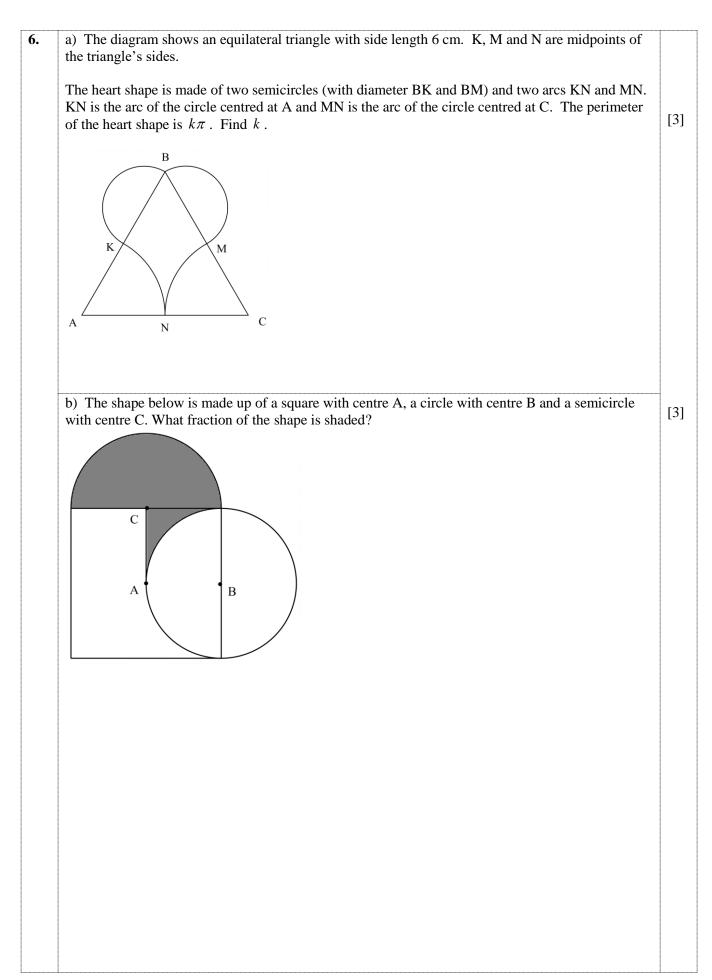
Please start Q4 on a new sheet of paper and write your name at the top.



Please start Q5 on a new sheet of paper and write your name at the top.

5.
$$a=3, b=-5 \text{ and } c=-11.$$

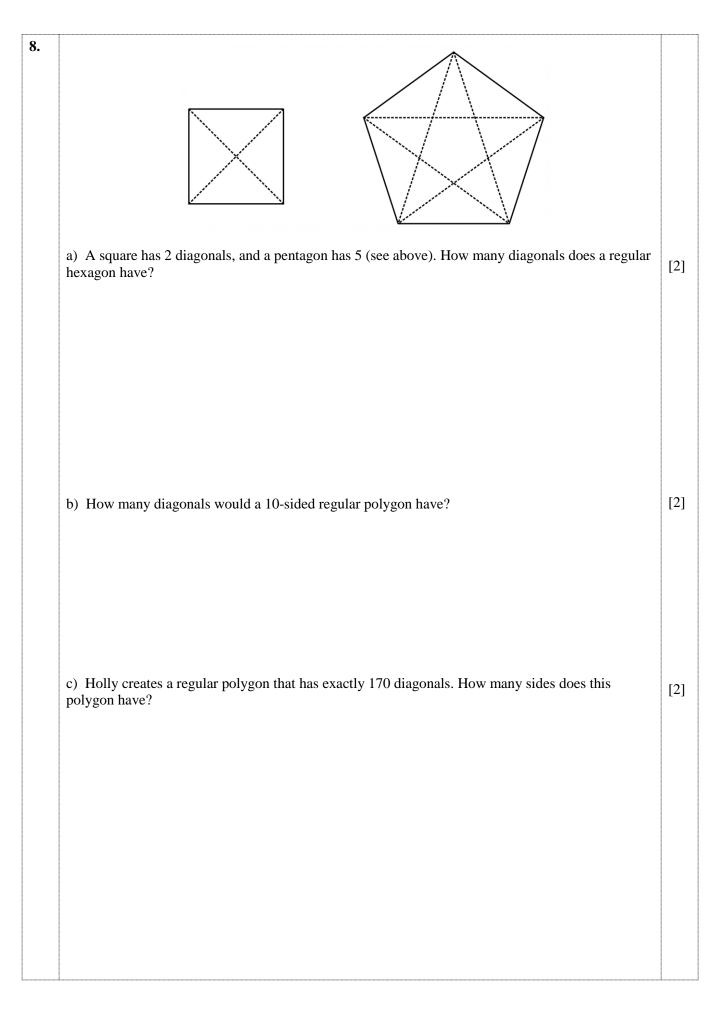
a) Evaluate $b^2 - 4ac.$
b) Evaluate $(a+b)(a^2 - ab + b^2)$.
c) Find $\left(a+\frac{1}{a}\right)^2$ as a mixed number in its
simplest form. Show it is not equal to $a^2 + \frac{1}{a^2}$.
(3) Evaluate $1 + a(2+3(b-(121+c)))$.
(3)
[2]



Please start Q7 on a new sheet of paper and write your name at the top.

7.	 a) Start with <i>x</i>. Add four. Multiply by two. Subtract one. Write down an expression that corresponds to these instructions and simplify your answer. 	b) Expand $(5a)^2 - 3(2a^2 - 15)$ and simplify.	[2]
	c) $\frac{16016}{b^3 - 11} = 1001$. Find <i>b</i> .	d) Solve $\frac{10}{1 - \frac{1}{1 + x}} = -5$.	[2]

Please start Q8 on a new sheet of paper and write your name at the top.



Please start Q9 on a new sheet of paper and write your name at the top.

r	1	r
9.	A mother has five children, Amy, Boris, Cara, David and Ezra. She says to each of them "I will give you an amount of money of your choosing up to ± 1000 . In addition, every year I shall give you one tenth of the amount of the ± 1000 that you did <i>not</i> take."	
	Amy chooses to receive £300. Next year she receives one tenth of £700 which is £70. The year after she receives another £70, and so after two years she has received, in total, £440.	
	a) Boris chooses to initially receive £200. How much does he receive, in total, after three years?	[2]
	b) Cara chooses to initially receive £400. After how many years has she received, in total, £760?	[2]

c) After nine years David wants to have the maximum possible amount. How much should he choose to initially receive?

d) After eleven years Ezra wants to have the maximum possible amount. How much should he choose to initially receive?

[2]

[2]

Please start Q10 on a new sheet of paper and write your name at the top.

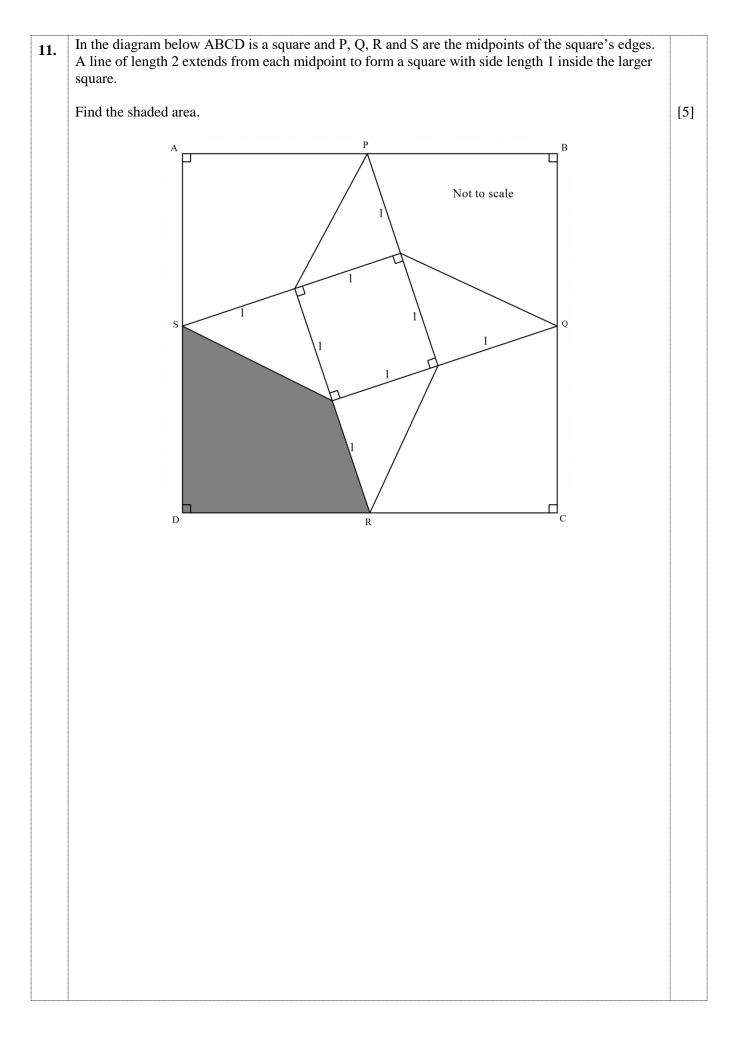
10		
10.	There are two ways to express 6 as a sum of two different positive whole numbers written in increasing order, namely $1+5$ and $2+4$.	
	a) List all the ways to express 11 as a sum of two different positive whole numbers written in increasing order.	[2]
	b) How many ways can 2021 be expressed as a sum of two different positive whole numbers written in increasing order?	[2]
	c) List all the ways to express 9 as a sum of three different positive whole numbers written in increasing order.	[2]

d) Alysha wants to express 99 as a sum of three different positive whole numbers written in	
increasing order, with the additional constraint that the mean of the numbers must be the same as	501
their median. How many ways can this be done?	[2]

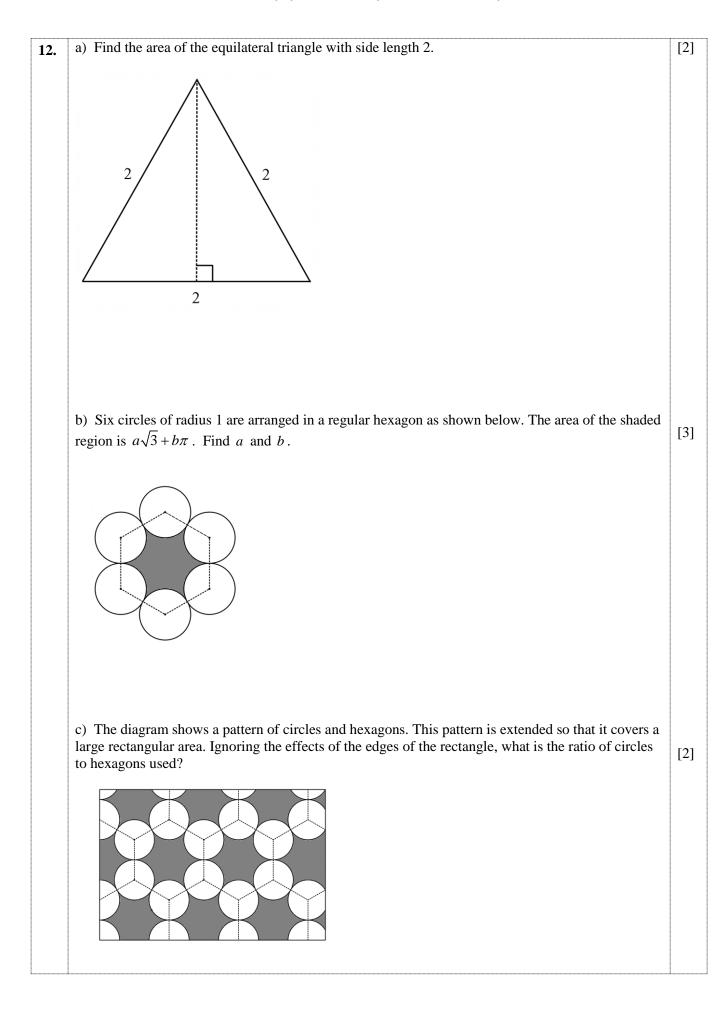
e) Bob wants to express 22 as a sum of four different numbers written in increasing order, with the additional constraint that the mean of the numbers must be the same as their median. How many ways can this be done?

[3]

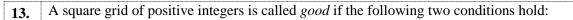
Please start Q11 on a new sheet of paper and write your name at the top.



Please start Q12 on a new sheet of paper and write your name at the top.

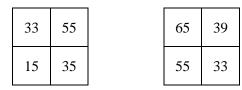


Please start Q13 on a new sheet of paper and write your name at the top.



- Each number in the grid is different and is a product of distinct odd primes less than 14.
- If two numbers are horizontally or vertically adjacent in the grid, then one can be transformed into the other by dividing by a prime and then multiplying by a different prime.

Below are two examples of good 2×2 grids.



a) Copy and complete the good grid below.

	77	
55		33
	91	

b) Find a number that is the product of two distinct odd primes less than 14 but does not appear in the grid. [1]

[4]

c) Copy and complete the good grid below.

	195	
273		455
	165	

d) Find a number that is the product of three distinct odd primes less than 14 but does not appear in the grid. [1]